

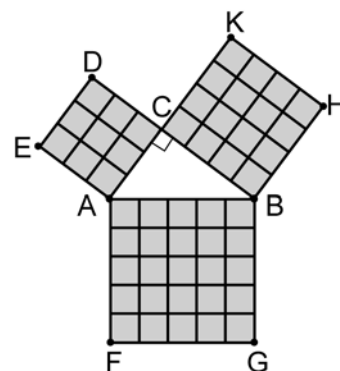
5C Pythagorean Theorem

Read:

The Pythagorean theorem states that the sum of the squares of the lengths of the legs of a right triangle is equal to the square of the hypotenuse. The following expression represents the Pythagorean theorem:

$a^2 + b^2 = c^2$ where c is the hypotenuse of a right triangle and a and b are the measures of the legs.

Geometrically, this theorem is that the area of $ABGF$ in the figure at right is equal to the sum of the areas of $ACDE$ and $BCKH$.



Examples:

Use the Pythagorean theorem expression ($a^2 + b^2 = c^2$) to solve the following

| | |
|--|---|
| <p>Example 1: What is the length of c if $a = 6$ and $b = 8$?</p> | $6^2 + 8^2 = c^2$ $36 + 64 = c^2$ $100 = c^2$ $\sqrt{100} = \sqrt{c^2}$ $10 = c$ |
| <p>Example 2: What is the length of a if $b = 5\sqrt{3}$ and $c = 10$?</p> | $a^2 + (5\sqrt{3})^2 = 10^2$ $a^2 + 75 = 100$ $a^2 = 25$ $\sqrt{a^2} = \sqrt{25}$ $a = 5$ |

problems.

Practice:

All of the following values apply to right triangles. Find the measure of the missing side of the triangle using the Pythagorean theorem. If the measure has a square root (like $\sqrt{3}$) leave it in the answer.

| | | | |
|----|-----------------|----------|-----------------|
| 1. | $a = 5$ | $b = 12$ | $c =$ |
| 2. | $a =$ | $b = 15$ | $c = 17$ |
| 3. | $a = 7$ | $b =$ | $c = 25$ |
| 4. | $a =$ | $b = 4$ | $c = 4\sqrt{2}$ |
| 5. | $a = 8\sqrt{3}$ | $b = 8$ | $c =$ |
| 6. | $a = 15$ | $b = 20$ | $c =$ |