

## 6A Adding Displacement Vectors

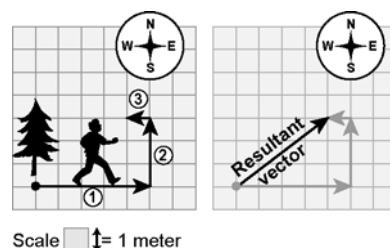
### Read:

A displacement vector is a quantity that contains two separate pieces of information: (1) magnitude or size, and (2) direction. When you add displacement vectors, you end up at a certain position. This new position is the total displacement from the original position. A vector that connects the starting position with the final position is called the resultant vector ( $x$ ).

### Example:

Andreas walked 5 meters east away from a tree. Then, he walked 3 meters north. Finally, he walked 1 meter west. Each of these three pathways is a displacement vector. Use these displacement vectors to find Andreas's total displacement from the tree.

| Displacement vector | Direction | Magnitude (meters) | Total magnitude (total meters walked) |
|---------------------|-----------|--------------------|---------------------------------------|
| 1                   | east      | 5                  | 5                                     |
| 2                   | north     | 3                  | $5 + 3 = 8$                           |
| 3                   | west      | 1                  | $8 + 1 = 9$                           |



Andreas's motion can be represented on a graph. To determine his total displacement from the tree, do the following:

- Add the east and west displacement vectors. These are in the  $x$ -axis direction on a graph.  
Andreas's walk = 5 m east + (- 1)m west = 4 m east
- Add the north and south displacement vectors. These are in the  $y$ -axis direction on a graph.  
Andreas's walk = 3 m north

The total displacement is 4 meters east and 3 meters north.

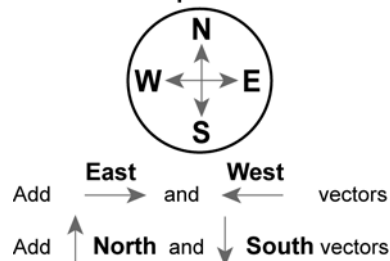
Andreas walked a total of 9 meters. The resultant vector ( $x$ ) goes from the starting position to the final position of total displacement.

- What is the total displacement of a bee that flies 2 meters east, 5 meters north, and 3 meters east?

- What is the total displacement of an ant that walks 2 meters west, 3 meters south, 4 meters east, and 1 meter north?

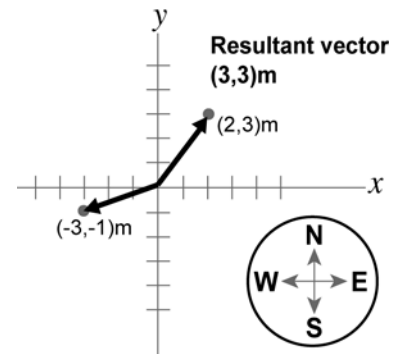
- A ball is kicked 10 meters north, 5 meters west, 15 meters south, 5 meters east, and 5 meters north. Find the total displacement and the total distance it traveled.

How to add displacement vectors:



## Adding displacement vectors using $x$ - $y$ coordinates

A resultant vector can be written using  $x$ - $y$  coordinates on a graph. The original position is the origin of a graph where the axes represent east-west and north-south positions. For example,  $(2,3)\text{m}$  is a resultant vector with the following components: 2 meters east and 3 meters north. A resultant vector,  $(-3,-1)\text{m}$ , has components 3 meters west and 1 meter south. Use this information to solve the following problems. Write your answers using  $x$ - $y$  coordinates.



### Example:

Add the following four vectors to find the resultant vector,  $x_R$ :

$$x_1 = (5,0)\text{m}, x_2 = (0,-5)\text{m}, x_3 = (3,0)\text{m}, x_4 = (-7,0)\text{m}$$

Add the east-west components: 5 m east + 0 m + 3 m east + (-7) m west = 1 m east

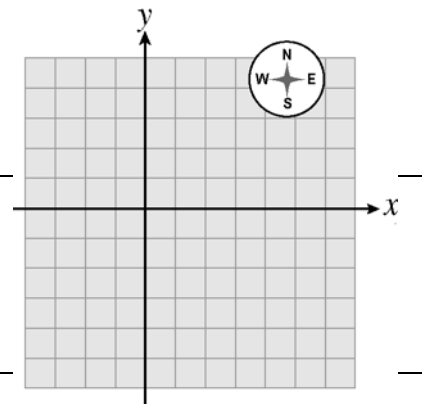
Add the north-south components: 0 m + (-5) m south + 0 m + 0 m = (-5) m south  $x_R = (1,-5)\text{m}$ .

1. Add the following three vectors to find the resultant vector,  $x_R$ :

$$x_1 = (-2,0)\text{m}, x_2 = (0,-5)\text{m}, x_3 = (3,0)\text{m}$$

2. Add the following vectors to find the resultant vector. Plot the resultant vector ( $x_R$ ) on the grid to the right:

$$x_1 = (4,0)\text{m}, x_2 = (-1,2)\text{m}, x_3 = (0,1)\text{m}$$



3. Add the following three vectors to find the resultant vector,  $x_R$ :

$$x_1 = (5,3)\text{m}, x_2 = (-5,0)\text{m}, x_3 = (5,2)\text{m}$$

4. Add the following three vectors to find the resultant vector,  $x_R$ :

$$x_1 = (6,-2)\text{m}, x_2 = (-3,1)\text{m}, x_3 = (3,3)\text{m}$$

5. Add the following three vectors to find the resultant vector,  $x_R$ :

$$x_1 = (4,4)\text{m}, x_2 = (-2,-6)\text{m}, x_3 = (0,2)\text{m}$$